For which values of a does the integral

$$\int_0^\infty x^{-a} \sin x dx$$

exist? explain carefully.