

2.2.15

$$y' = \frac{2x}{1+2y}, y(2) = 0$$

$y \neq -\frac{1}{2}$

1.3: 3, 4, 11  
2.1: 12, 16, 18, 20  
2.2: 5, 7, 15, 21  
2.3: 5, 12, 18

(a)  $\int (1+2y) dy = \int 2x dx$  (1/2) (c)

$$y^2 + y = x^2 + C$$

$y(2) = 0: 0^2 + 0 = 2^2 + C$   
 $C = -4$

$$y^2 + y = x^2 - 4$$

$$y^2 + y + 4 - x^2 = 0$$

$$y = \frac{-1 \pm \sqrt{1^2 - 4(4-x^2)}}{2(1)}$$

$$= -\frac{1}{2} \pm \frac{\sqrt{4x^2 - 15}}{2}$$

With  $y(2) = 0$ :

$$y = -\frac{1}{2} + \frac{\sqrt{4x^2 - 15}}{2}$$

$$4x^2 - 15 \geq 0$$

$$x^2 \geq \frac{15}{4}$$

$$|x| \geq \frac{\sqrt{15}}{2}$$

But  $|x| \neq \frac{\sqrt{15}}{2}$ , otherwise

$$4x^2 - 15 = 0$$

and  $y = -\frac{1}{2}$

So  $|x| > \frac{\sqrt{15}}{2}$ , i.e.,

$$x < -\frac{\sqrt{15}}{2}$$

or  $x > \frac{\sqrt{15}}{2}$

must include initial value of  $x, y$ ,  $x=2$

