Maximal Vertex-Connectivity of $\overrightarrow{A_{n,k}}$

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Abstract

Arrangement graph $A_{n,k}$ has a vertex set labeled by all the arrangements of k elements chosen from the ground set $\{1, 2, ..., n\}$. Two vertices are adjacent if their labels differ in exactly one of the k positions. $A_{n,k}$ contains both Star S_n and Alternating Group A_n graphs as special cases. $A_{n,n-1} \cong S_n$ which was proposed as an alternative to hypercube Q_n , while $A_{n,n-2} \cong A_n$.

This talk presents modification to orientation of Arrangement graph previously given by Cheng and Lippman, and shows that a consequence of such an orientation is that unidirectional $A_{n,k}$ becomes maximally connected, that is $\overrightarrow{A_{n,k}}$ is r-connected, where $r = \min_{v \in V} \{\rho(v), \delta(v)\}$.